## Package: kitagawa (via r-universe)

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Type Package

**Title** Spectral Response of Water Wells to Harmonic Strain and Pressure Signals

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**Description** Provides tools to calculate the theoretical hydrodynamic response of an aquifer undergoing harmonic straining or pressurization, or analyze measured responses. There are two classes of models here, designed for use with confined aquifers: (1) for sealed wells, based on the model of Kitagawa et al (2011, <doi:10.1029/2010JB007794>), and (2) for open wells, based on the models of Cooper et al (1965, <doi:10.1029/JZ070i016p03915>), Hsieh et al (1987, <doi:10.1029/WR023i010p01824>), Rojstaczer (1988, <doi:10.1029/JB093iB11p13619>), Liu et al (1989, <doi:10.1029/JB094iB07p09453>), and Wang et al (2018, <doi:10.1029/2018WR022793>). Wang's solution is a special exception which allows for leakage out of the aguifer (semi-confined); it is equivalent to Hsieh's model when there is no leakage (the confined case). These models treat strain (or aquifer head) as an input to the physical system, and fluid-pressure (or water height) as the output. The applicable frequency band of these models is characteristic of seismic waves, atmospheric pressure fluctuations, and solid earth tides.

**License** GPL (>= 2)

URL https://github.com/abarbour/kitagawa

BugReports https://github.com/abarbour/kitagawa/issues

**Depends** R (>= 2.10.1), stats

**Imports** Bessel, kelvin (>= 1.2.0), psd (>= 2.0.0)

**Suggests** dplyr, tibble, RColorBrewer, signal, testthat, knitr, rmarkdown, formatR, covr

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## VignetteBuilder knitr

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alpha	ha constants Calculate any constants depending on a	effective stress coefficient α	

## Description

This function accesses the appropriate method to calculate the  $\alpha$ -dependent constant associated with the choice of c. type. There are currently four such constants, which correspond to **Equations 10**, **11**, **18**, **19** in Kitagawa et al (2011).

This function is not likely to be needed by the user.

## Usage

```
alpha_constants(alpha = 0, c.type = c("Phi", "Psi", "A", "Kel"))
## Default S3 method:
alpha_constants(alpha = 0, c.type = c("Phi", "Psi", "A", "Kel"))
```

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#### **Arguments**

alpha the constant alpha (see omega\_constants)

c. type the constant to calculate

#### **Details**

What is "alpha"?: The constant  $\alpha$  is a function of frequency  $\omega$  as well as aquifer and well parameters; it is formally defined as

$$\alpha \equiv R_S \sqrt{\omega S/T}$$

where S is the storativity, T is the aquifer's effective transmissivity, and  $R_S$  is the radius of the screened portion of the well.

What is calculated?: The various constants which may be calculated with this function are

```
Phi Given as \Phi in Eqn. 10
Psi Given as \Psi in Eqn. 11
A Given as A_i, i=1,2 in Eqns. 18, 19
Kel The complex Kelvin functions (see Abramowitz and Stegun, 1972)
```

#### Value

Complex matrix having values representing the constant represented by c.type, as well as any other  $\alpha$ -dependent constants which are needed in the computation.

#### Author(s)

A. J. Barbour <andy.barbour@gmail.com>

#### See Also

```
omega_constants, well_response
Other ConstantsCalculators: kitagawa-constants, omega_constants()
```

## **Examples**

```
alpha_constants()  # kelvin::Keir gives warning
alpha_constants(1)  # defaults to constant 'Phi' (note output also has Kel)
alpha_constants(1:10, c.type="A")  # constant 'A' (again, note output)
```

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 ${\tt cross\_spectrum}$ 

Calculate the cross-spectrum of two timeseries

## Description

Calculate the cross-spectrum of two timeseries

## Usage

```
cross_spectrum(x, ...)
## S3 method for class 'mts'
cross_spectrum(x, ...)
## Default S3 method:
cross_spectrum(
    x,
    y,
    k = 10,
    samp = 1,
    q,
    adaptive = FALSE,
    verbose = FALSE,
    ...
)
```

## Arguments

X	numeric; timeseries
	additional arguments to pspectrum
У	numeric; timeseries. if missing, assumed to be column no. 2 in x
k	integer; the number of sine tapers, unless this is NULL; in the latter case a Welchbased spectrum is calculated rather than a multitaper spectrum. There are distinct advantages and disadvantages to either of these.
samp	numeric; the sampling rate (e.g., $deltat$ ) of the data; must be the same for x and y
q	numeric; the probability quantile $[0,1]$ to calculate coherence significance levels; if missing, a pre-specified sequence is included. This is will be ignored for Welch-based spectra (see k).
adaptive	logical; should adaptive multitaper estimation be used?
verbose	logical; should messages be printed?

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#### **Examples**

```
require(stats)
require(psd)

n <- 1000
ramp <- seq_len(n)
parab <- ramp^2

set.seed(1255)
X <- ts(rnorm(n) + ramp/2)
Y <- ts(rnorm(n) + ramp/10 + parab/100)

# Calculate the multitaper cross spectrum
csd <- cross_spectrum(X, Y, k=20)</pre>
```

kitagawa-constants

Access to constants used by default

## Description

The response of an aquifer depends on its mechanical and hydrological properties; if these are not known or specified, these constants are used.

## Usage

```
constants(do.str = TRUE)
```

## **Arguments**

do.str

logical; should the structure be printed?

#### **Details**

The function constants shows the structure of (optionally), and returns the assumed constants, which do *not* reside in the namespace.

#### Values:

For water: Density and bulk modulus

**Gravity:** Standard gravitational acceleration at 6371km radius (Earth)

**Conversions:** Degrees to radians

#### Value

The constants, invisibly.

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#### See Also

```
well_response and open_well_response
kitagawa-package
Other ConstantsCalculators: alpha_constants(), omega_constants()
```

## **Examples**

```
constants()
constants(FALSE) # returns invisibly
```

kitagawa-utilities

General utility functions

## Description

General utility functions

## Usage

```
.nullchk(X)
.in0to1(X)
is.wrsp(X)
is.owrsp(X)
```

## Arguments

Χ

something to be checked (vector, scalar, wrsp object, ...)

#### **Details**

.nullchk quickly checks for NULL and NA, and raises an error if TRUE; *This function is not likely to be needed by the user.* 

. in0to1 checks if values are numeric and in [0,1] (inclusive).

is.wrsp and is.owrsp report whether an object has S3 class 'wrsp' or 'owrsp', respectively. Such an object would be returned by, for example, well\_response.

#### Author(s)

A. J. Barbour <andy.barbour@gmail.com>

#### See Also

```
kitagawa-package
```

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#### **Examples**

```
## Not run:
.nullchk(1:10) # OK
.nullchk(NULL) # error
.nullchk(c(1:10,NULL)) # error
.nullchk(NA) # error
.nullchk(c(1:10,NA)) # error
.in0to1(1:10) # error
.in0to1(NULL) # error
.in0to1(c(1:10,NULL)) # error
.in0to1(NA) # error
.in0to1(c(1:10,NA)) # error
.in0to1(c(1:10,NA)) # error
.in0to1(c(1,NA)) # error
.in0t
```

logsmoo

Logarithmic smoothing with loess

## Description

Logarithmic smoothing with loess

#### Usage

```
logsmoo(x, y, x.is.log = FALSE, ...)
```

#### **Arguments**

```
    x numeric; the index series (cannot contain NA)
    y numeric; the series of values associated with x
    x.is.log logical; determines whether the series in x has been log-transformed already. If FALSE then log10 is used.
    additional parameters (e.g., span) passed to loess.smooth
```

#### Value

The result of loess. smooth

#### References

Barbour, A. J., and D. C. Agnew (2011), Noise levels on Plate Boundary Observatory borehole strainmeters in southern California, Bulletin of the Seismological Society of America, 101(5), 2453-2466, doi: 10.1785/0120110062

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#### See Also

loess.smooth and approxfun

#### **Examples**

```
set.seed(11133)
n <- 101
lx <- seq(-1,1,length.out=n)
y <- rnorm(n) + cumsum(rnorm(n))
plot(lx, y, col='grey')
lines(logsmoo(lx, y, x.is.log=TRUE))</pre>
```

logticks

Add proper logarithm ticks to a plot axis.

## Description

Add proper logarithm ticks to a plot axis.

## Usage

```
logticks(
    ax = 1,
    n.minor = 9,
    t.lims,
    t.ratio = 0.5,
    major.ticks = NULL,
    base = c("ten", "ln", "two"),
    ticks.only = FALSE,
    ...
)
log_ticks(...)
log2_ticks(...)
```

## **Arguments**

```
ax numeric; the axis number to add tick-marks to

n.minor numeric; the number of minor ticks to display

t.lims numeric; the upper and lower tick limits (in log space)

t.ratio numeric; the ratio of minor to major tick lengths.

major.ticks numeric; the axis limits.
```

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base numeric; the base of the logarithm (somewhat experimental)

ticks.only logical; on the axis

... additional parameters passed to the axis call for the major ticks.

#### **Details**

This uses pretty with n==5, and assumes that the data along the axis ax has *already* been transformed into its logarithm. *Only integer exponents are labeled*.

The functions log\_ticks, log2\_ticks, and log10\_ticks are wrapper functions.

Set the axt parameter (e.g. xaxt) to 'n' in the original plot command to prevent adding default tick marks.

#### Author(s)

A. J. Barbour <andy.barbour@gmail.com>

#### References

This was modified from a post on StackOverflow: https://stackoverflow.com/questions/6955440/displaying-minor-logarithmic-ticks-in-x-axis-in-r

#### See Also

Other PlotUtilities: wrsp-methods

## **Examples**

```
x <- 10^(0:8)
y <- 1:9

plot(log10(x),y,xaxt="n",xlab="x",xlim=c(0,9))
logticks()
logticks(ax=3, ticks.only=TRUE)

par(tcl=0.5) # have tick marks show up on inside instead
plot(log10(x),y,xaxt="n",xlab="x",xlim=c(0,9))
logticks()
logticks(ax=3, ticks.only=TRUE)</pre>
```

omega\_constants

Calculate any constants that depend on angular frequency  $\omega$ 

#### **Description**

This function accesses the appropriate method to calculate the  $\omega$ -dependent constant associated with the choice of c. type.

This function is not likely to be needed by the user.

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#### Usage

```
omega_constants(omega = 0, c.type = c("alpha", "diffusivity_time"), ...)
## Default S3 method:
omega_constants(omega = 0, c.type = c("alpha", "diffusivity_time"), ...)
```

#### **Arguments**

omega	frequency, $[rad/sec]$
c.type	the constant to calculate
	additional params passed to calculator. In the case of ctype="alpha", set S., T., Rs.; and, in the case of ctype="diffusivity_time", set D. or S., T

#### Details

What is "omega"?: The name is in reference to radial frequency  $\omega$ , which is defined as

$$\omega \equiv 2\pi/\tau$$

where  $\tau$  is the period of oscillation.

## What is the "alpha" calculation?:

The parameter  $\alpha$  is defined as

$$\alpha \equiv r_w \sqrt{\omega S/T}$$

where  $r_w$  is the radius of the well, where S is the storativity, and T is transmissivity. See the parameter . . . for details on how to pass these values.

This definition is common to many papers on the topic. For example, it corresponds to **Equation 12** in Kitagawa et al (2011). Because the computation of  $\alpha$  depends also on physical properties, additional parameters can be passed through (e.g. the transmissivity).

What is the "diffusivity\_time" calculation?: This is a similar calculation to omega\_norm. It uses the effective hydraulic diffusivity D, which is defined in this case as the ratio of transmissivity to storativity:

$$D \equiv \frac{T}{S}$$

#### Value

Values of the constant represented by c. type for the given parameters

## **Warnings Issued**

In the case c.type='alpha', the parameters S., T., and Rs. should be passed; otherwise, values are assumed to ensure the calculation does not fail, and the results are essentially meaningless.

Warnings will be issued if any necessary parameters are missing, indicating default values were used.

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#### Author(s)

A. J. Barbour <andy.barbour@gmail.com>

#### See Also

alpha\_constants, well\_response, and kitagawa-package for references and more background. Other ConstantsCalculators: alpha\_constants(), kitagawa-constants

## **Examples**

```
# alpha
omega_constants() # default is alpha, but will give warnings about S., T., Rs.
omega_constants(T.=1,S.=1,Rs.=1) # 0, no warnings
omega_constants(1:10) # sequence, with warnings about S., T., Rs.
omega_constants(1:10,T.=1,S.=1,Rs.=1) # sequence, no warnings
# diffusivity time
omega_constants(c.type="diffusivity_time", D.=1) # 0, no warnings
omega_constants(c.type="diff", D.=1) # 0, no warnings (arg matching)
omega_constants(c.type="diff") # 0, warnings about S., T. because no D.
omega_constants(c.type="diff", S.=1) # 0, warnings about T. because no D. or S.
```

omega\_norm

Dimensionless frequency from diffusivity and depth

## Description

Dimensionless frequency from diffusivity and depth

## Usage

```
omega_norm(omega, Diffusiv, z, invert = FALSE)
```

#### **Arguments**

omega numeric; angular frequency
Diffusiv numeric; hydraulic diffusivity

z numeric; depth

invert logical; should omega be taken as normalized frequency?

#### **Details**

Dimensionless frequency Q is defined as

$$Q = \frac{z^2 \omega}{2D}$$

where z is the well depth,  $\omega$  is the angular frequency and D is the hydraulic diffusivity.

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## Value

omega\_norm returns dimensionless frequency, unless invert=TRUE where it will assume omega is dimensionless frequency, and return radial frequency.

#### Author(s)

A. J. Barbour <andy.barbour@gmail.com>

## See Also

```
open_well_response, kitagawa-package
Other utilities: sensing_volume()
```

open\_well\_response

Spectral response for an open well

## Description

This is the primary function to calculate the response for an open (exposed to air) well.

## Usage

```
open_well_response(omega, T., S., ...)
## Default S3 method:
open_well_response(
 omega,
 Τ.,
  S.,
 Rs. = (8/12) * (1200/3937),
  rho,
  grav,
  Ζ,
 Hw,
  Тa,
  leak,
  freq.units = c("rad_per_sec", "Hz"),
 model = c("rojstaczer", "liu", "cooper", "hsieh", "wang"),
 as.pressure = TRUE,
)
```

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## Arguments

omega	numeric; frequency, (see freq.units)
T.	numeric; effective aquifer transmissivity $[m^2/s]$
S.	numeric; well storativity, [unitless]
• • •	additional arguments
Rs.	numeric; the radius of the open (screened) section
rho	numeric; fluid density (assumed if missing)
grav	numeric; the local gravitational acceleration (assumed if missing)
z	numeric; From Rojstaczer (1988): the depth from the water table (assumed if missing and if needed)
Hw	numeric; height of water column above confined surface (assumed if missing and if needed)
Та	numeric; thickness of aquifer (assumed if missing and if needed)
leak	numeric; specific leakage $K'/b'$ [1/s]
freq.units	character; setup the units of omega
mode1	character; use the response model from either Rojstaczer (1988), Liu et al (1989), Cooper et al (1965), Hsieh et al (1987), or Wang et al (2018).
as.pressure	logical; should the response be relative to aquifer pressure? (default is aquifer

### Details

As opposed to well\_response, this calculates the theoretical, complex well response for an unsealed (open) well.

The response depends strongly on the physical properties given. Default values are assumed where reasonable—for instance, the pore-fluid is assumed to be water—but considerable care should be invested in the choice of parameters, especially in the case of starting parameters in an optimization scheme.

The responses returned here are, effectively, the amplification of water levels in a well, relative to the pressure head in the aquifer; or

 $Z=\frac{z}{h}\equiv\frac{\rho gz}{p}$ 

If as.pressure=TRUE, then the responses are scaled by rho\*grav so that they represent water levels relative to aquifer pressure:

 $Z = \frac{z}{p}$ 

Not all parameters need to be given, but should be. For example, if either rho or grav are not specified, they are taken from constants. Parameters which do not end in . do not need to be specified (they may be excluded); if they are missing, assumptions may be made and warnings will be thrown.

#### Value

An object with class 'owrsp'

head)

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#### Models

"rojstaczer": Rojstaczer (1988) is based on measurements of water level and strain from volumetric or areal strainmeters.

"cooper", "hsieh", and "liu": Cooper et al (1965), Hsieh et al (1987) and Liu et al (1989) are based on measurements of water level and displacements from seismometers or strainmeters; these models are expressed succinctly in Roeloffs (1996).

The sense of the phase shift for the Liu and Rojstaczer models are reversed from their original presentation, in order to account for differences in sign convention.

"wang": Wang et al (2018) allows for specific leakage – vertical conductivity across a semipermeable aquitard – but the perfectly confined case (i.e., Hsieh, et al 1987) is recovered when leakage is zero.

#### Author(s)

A. J. Barbour and J. Kennel

#### References

See kitagawa-package for references and more background.

#### See Also

well\_response for the sealed-well equivalents, and owrsp-methods for a description of the class 'owrsp' and its methods.

Other WellResponseFunctions: well\_response()

## **Examples**

```
OWR <- open_well_response(1:10,1,1)
plot(OWR)
OWR <- open_well_response(1/(1:200),1,1,Ta=100,Hw=10,model="liu",freq.units="Hz")
plot(OWR)</pre>
```

owrsp-methods

Generic methods for objects with class 'owrsp'.

#### **Description**

An object with class 'owrsp' is a list containing the response information, and the mechanical, hydraulic, and material properties used to generate the response for an open well.

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#### Usage

```
## S3 method for class 'owrsp'
as.data.frame(x, ...)
data.frame.owrsp(x, ...)
## S3 method for class 'owrsp'
print(x, n = 3, ...)
## S3 method for class 'owrsp'
summary(object, ...)
## S3 method for class 'summary.owrsp'
print(x, ...)
## S3 method for class 'owrsp'
lines(x, series = c("amp", "phs"), ...)
## S3 method for class 'owrsp'
points(x, series = c("amp", "phs"), pch = "+", ...)
## S3 method for class 'owrsp'
plot(
  Х,
  xlims = c(-3, 1),
  ylims = list(amp = NULL, phs = 185 * c(-1, 1)),
  logamp = TRUE,
)
```

### **Arguments**

```
'owrsp' object
Χ
                   optional arguments
                   numeric; the number of head and tail to print
object
                   'owrsp' object
                   character; the series to plot (amplitude or phase)
series
                   point character, as in par
pch
                   limits for x-axis (applies to both amp and phs frames)
xlims
                   optional list of limits for y-axis (i.e., list(amp=c(...), phs=c(...)))
ylims
                   logical; should the amplitude be in log10 units
logamp
```

#### **Details**

The response information is a matrix with frequency, complex response  $[\omega, Z_{\alpha}(\omega)]$  where the units of  $\omega$  will be as they were input. The amplitude of Z is in meters per strain, and the phase is in radians.

sensing\_volume

#### Author(s)

A. J. Barbour <andy.barbour@gmail.com>

#### See Also

```
open_well_response
kitagawa-package
```

#### **Examples**

```
S. <- 1e-5 # Storativity [nondimensional]</pre>
T. <- 1e-4 # Transmissivity [m**2 / s]
frq <- 1/(1:200)
# Defaults to the Rojstaczer formulation
W <- open_well_response(frq, T. = T., S. = S., Rs. = 0.12, freq.units="Hz")
# (warning message about missing 'z')
W <- open_well_response(frq, T. = T., S. = S., Rs. = 0.12, freq.units="Hz", z=1)
str(W)
print(W)
print(summary(W))
plot(rnorm(10), xlim=c(-1,11), ylim=c(-2,2))
lines(W, "phs", col="red")
points(W)
points(W, "phs")
Wdf <- as.data.frame(W)</pre>
plot(Mod(wellresp) ~ omega, Wdf) # amplitude
plot(Arg(wellresp) ~ omega, Wdf) # phase
plot(W)
# change limits:
plot(W, xlims=c(-4,0), ylims=list(amp=c(-7,-3), phs=185*c(-1,1)))
```

sensing\_volume

Calculate volume of fluids in the sensing region of the borehole.

#### **Description**

This function calculates the volume of fluid in the screened section, namely **Equation 2** in Kitagawa et al (2011).

#### Usage

```
sensing_volume(rad_grout, len_grout, rad_screen, len_screen)
```

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#### **Arguments**

```
 \begin{array}{lll} {\rm rad\_grout} & {\rm radius~of~the~grouting}~[m] \\ {\rm length~of~the~grouting}~[m] \\ {\rm rad\_screen} & {\rm radius~of~the~screened~interval}~[m] \\ {\rm len\_screen} & {\rm length~of~the~screened~interval}~[m] \\ \end{array}
```

#### **Details**

Although typical scientific boreholes with water-level sensors are drilled very deeply, pore-fluids are only allowed to flow through a relatively short section, known as the "screened" section. The calculation assumes two pairs of radii and lengths: one for the cemented (grout) section, and another for the screened section.

The volume calculated is

$$\pi R_C^2 (L_C - L_S) + \pi R_S^2 L_S$$

where R and L denote radius and length respectively, and subscripts C and S denote the cemented and screened sections respectively.

This calculation assumes the measurement is for a sealed well.

#### Value

```
scalar, with units of [m^3]
```

#### Author(s)

A. J. Barbour <andy.barbour@gmail.com>

#### See Also

```
well_response
Other utilities: omega_norm()
```

## Examples

```
#### dummy example
sensing_volume(1, 1, 1, 1)
#
##### a more physically realistic calculation:
# Physical params applicable for B084 borehole
# (see: http://pbo.unavco.org/station/overview/B084/ for details)
#
Rc <- 0.0508  # m, radius of water-sensing (2in)
Lc <- 146.9  # m, length of grouted region (482ft)
Rs <- 3*Rc  # m, radius of screened region (6in)
Ls <- 9.14  # m, length of screened region (30ft)
#
# calculate the sensing volume for the given well parameters
sensing_volume(Rc, Lc, Rs, Ls) # m**3, ~= 1.8</pre>
```

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well\_response

Spectral response for a sealed well

## Description

This is the primary function to calculate the response for a sealed well.

## Usage

```
well_response(omega, T., S., Vw., Rs., Ku., B., ...)
## Default S3 method:
well_response(
  omega,
  Τ.,
  S.,
  Vw.,
  Rs.,
  Ku.,
  В.,
  Avs,
  Αw,
  rho,
  Kf,
  grav,
  freq.units = c("rad_per_sec", "Hz"),
  as.pressure = TRUE,
)
```

## **Arguments**

```
frequency, (see freq.units)
omega
Τ.
                   effective aquifer transmissivity [m^2/s]
                   well storativity, [unitless]
S.
                   well volume, [m^3]
Vw.
                   radius of screened portion, [m]
Rs.
                   undrained bulk modulus, [Pa]
Ku.
                   Skempton's coefficient, [unitless, bounded]
В.
                   additional arguments
. . .
                   amplification factor for volumetric strain E_{kk,obs}/E_{kk}, []
Avs
                   amplification factor of well volume change for E_{kk}, []
Αw
                   fluid density [kg/m^3]
rho
                   bulk modulus of fluid, [Pa]
Κf
```

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grav local gravitational acceleration  $[m/s^2]$ 

freq.units set the units of omega

as.pressure logical; should the response for water pressure? (default is water height)

#### **Details**

The response depends strongly on the physical properties given. Default values are assumed where reasonable—for instance, the pore-fluid is assumed to be water—but considerable care should be invested in the choice of parameters, unless the function is used in an optimization scheme.

Assumed values are:

Avs 1 amplification factor for volumetric strain Aw 1 amplification factor for water well

The responses returned here are, effectively, the amplification of water levels in a well, relative to the aquifer strain; or

$$Z = \frac{z}{\epsilon} \equiv \frac{p}{\rho g \epsilon}$$

If as.pressure=TRUE, then the responses are scaled by rho\*grav so that they represent water pressure relative to aquifer strain:

$$Z = \frac{p}{\epsilon}$$

Not all parameters need to be given, but should be. For example, if either rho or grav are not specified, they are taken from constants. *Parameters which do not end in . do not need to be specified (they may be excluded); if they are missing, warnings will be thrown.* 

#### Value

An object with class 'wrsp'

#### Author(s)

A. J. Barbour

#### References

See kitagawa-package for references and more background.

#### See Also

open\_well\_response for the open-well equivalents wrsp-methods for a description of the class 'wrsp' and its methods, sensing\_volume to easily estimate the volume Vw., and kitagawa-package for references and more background.

Other WellResponseFunctions: open\_well\_response()

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#### **Examples**

```
#### dummy example
well_response(1:10, T.=1, S.=1, Vw.=1, Rs.=1, Ku.=1, B.=1)
#### a more physically realistic calculation:
# Physical params applicable for B084 borehole
# (see: http://pbo.unavco.org/station/overview/B084/ for details)
Rc <- 0.0508 # m, radius of water-sensing (2in)
Lc <- 146.9
              # m, length of grouted region (482ft)
              # m, radius of screened region (6in)
Rs <- 3*Rc
Ls <- 9.14
              # m, length of screened region (30ft)
# calculate the sensing volume for the given well parameters
Volw <- sensing_volume(Rc, Lc, Rs, Ls) # m**3, ~= 1.8</pre>
Frgs <- 10**seq.int(from=-4,to=0,by=0.1) # log10-space
head(Rsp <- well_response(omega=Frqs, T.=1e-6, S.=1e-5,
Vw.=Volw, Rs.=Rs, Ku.=40e9, B.=0.2, freq.units="Hz"))
# Access plot.wrsp:
plot(Rsp)
```

wrsp-methods

Generic methods for objects with class 'wrsp'.

## Description

An object with class 'wrsp' is a list containing the response information, and the mechanical, hydraulic, and material properties used to generate the response for a sealed well.

#### Usage

```
## S3 method for class 'wrsp'
as.data.frame(x, ...)

data.frame.wrsp(x, ...)

## S3 method for class 'wrsp'
print(x, n = 3, ...)

## S3 method for class 'wrsp'
summary(object, ...)

## S3 method for class 'summary.wrsp'
print(x, ...)
```

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```
## S3 method for class 'wrsp'
lines(x, series = c("amp", "phs"), ...)
## S3 method for class 'wrsp'
points(x, series = c("amp", "phs"), pch = "+", ...)
## S3 method for class 'wrsp'
plot(
 х,
 xlims = c(-3, 1),
 ylims = list(amp = NULL, phs = 185 * c(-1, 1)),
 logamp = TRUE,
)
kitplot(x, ...)
## S3 method for class 'wrsp'
kitplot(
  х,
 xlims = c(-3, 1),
 ylims = list(amp = NULL, phs = 185 * c(-1, 1)),
 logamp = TRUE,
)
```

## Arguments

X	'wrsp' object
	optional arguments
n	numeric; the number of head and tail to print
object	'wrsp' object
series	character; the series to plot (amplitude or phase)
pch	point character, as in par
xlims	limits for x-axis (applies to both amp and phs frames)
ylims	optional list of limits for y-axis (i.e., list(amp=c(), phs=c()))
logamp	logical; should the amplitude be in log10 units

#### **Details**

The response information is a matrix with frequency, complex response  $[\omega, Z_{\alpha}(\omega)]$  where the units of  $\omega$  will be as they were input. The amplitude of Z is in meters per strain, and the phase is in radians.

kitplot was previously a standalone function, but is now simply a reference to plot.wrsp.

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#### See Also

```
well_response
kitagawa-package
Other PlotUtilities: logticks()
```

## **Examples**

```
W <- well_response(1:10, T.=1, S.=1, Vw.=1, Rs.=1, Ku.=1, B.=1)
str(W)
print(W)
print(summary(W))
# Plot the response
plot(rnorm(10), xlim=c(-1,11), ylim=c(-2,2))
lines(W)
lines(W, "phs", col="red")
points(W)
points(W, "phs")
Wdf <- as.data.frame(W)</pre>
plot(Mod(wellresp) ~ omega, Wdf) # amplitude
plot(Arg(wellresp) ~ omega, Wdf) # phase
# or use the builtin method plot.wrsp
plot(W)
# change limits:
plot(W, xlims=c(-1,1), ylims=list(amp=c(5,8), phs=185*c(-1,1)))
```

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